

# Resource Allocation for Hardware Implementations of Map

Richard Townsend

Martha A. Kim

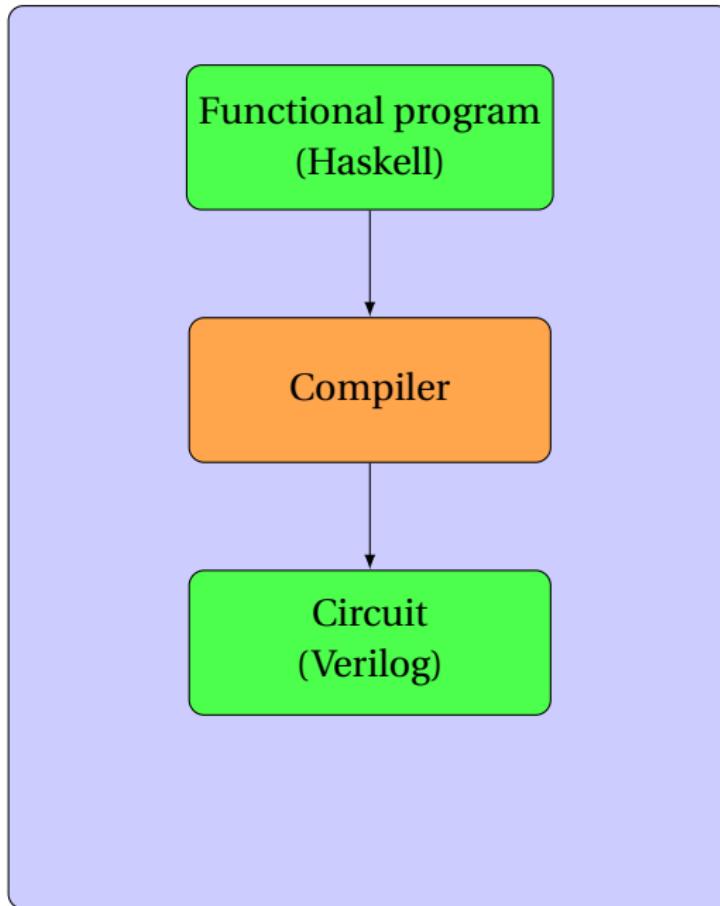
Stephen A. Edwards

Columbia University

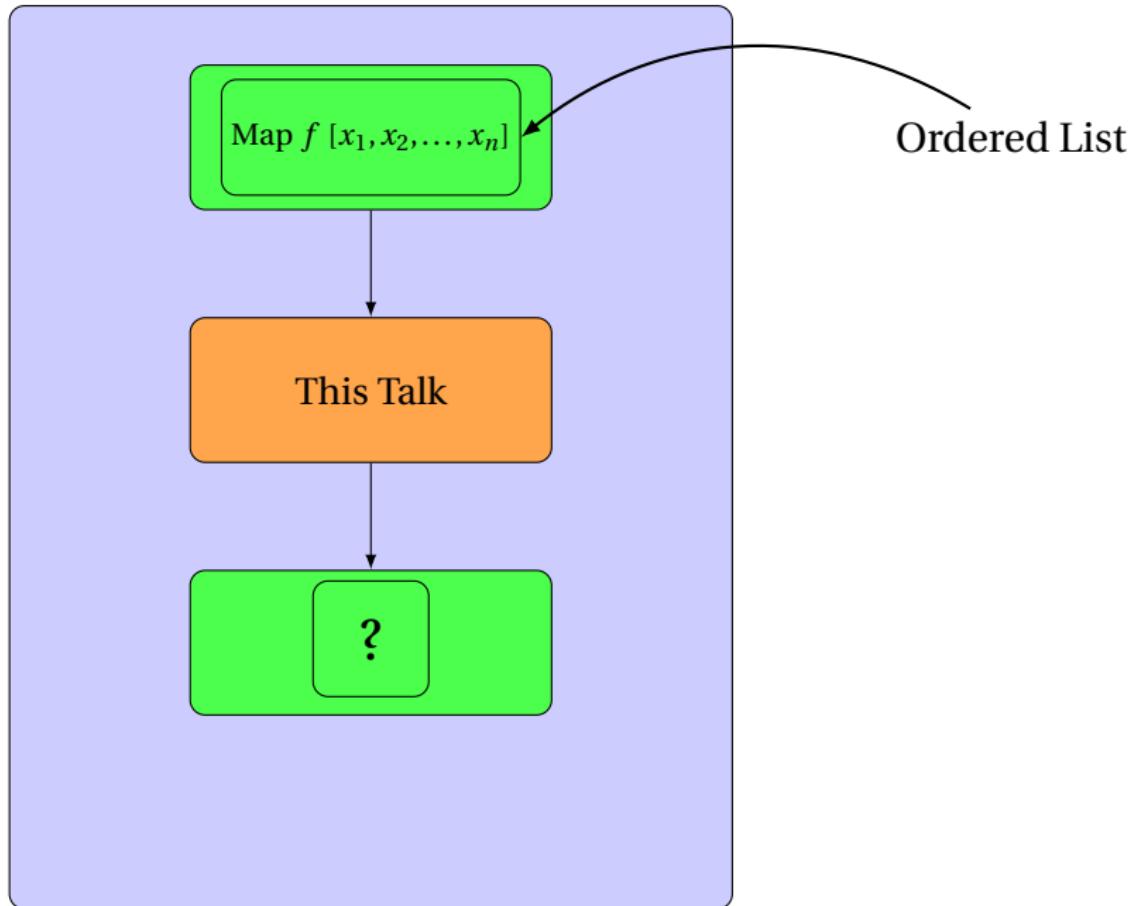
ASBD Workshop, June 15, 2014



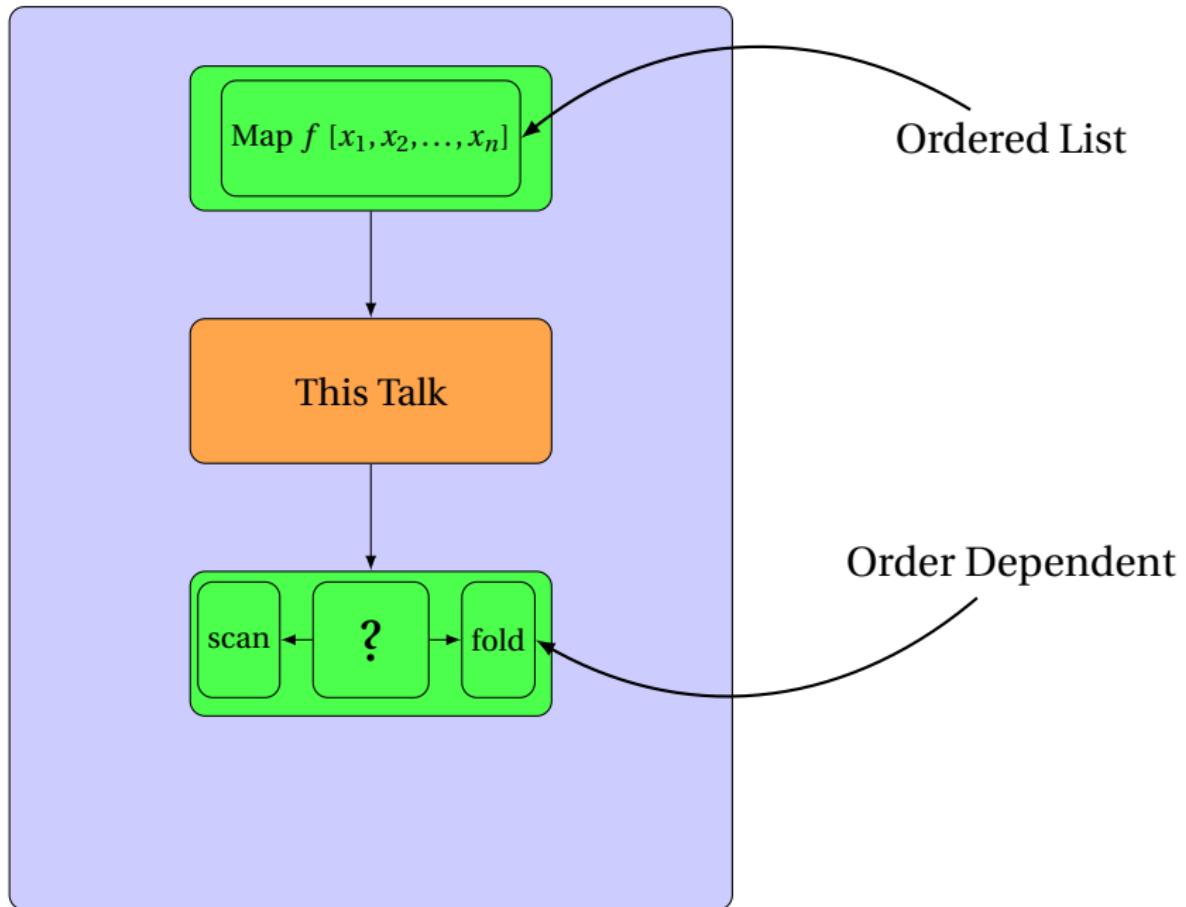
# Functional Programs to Functional Hardware



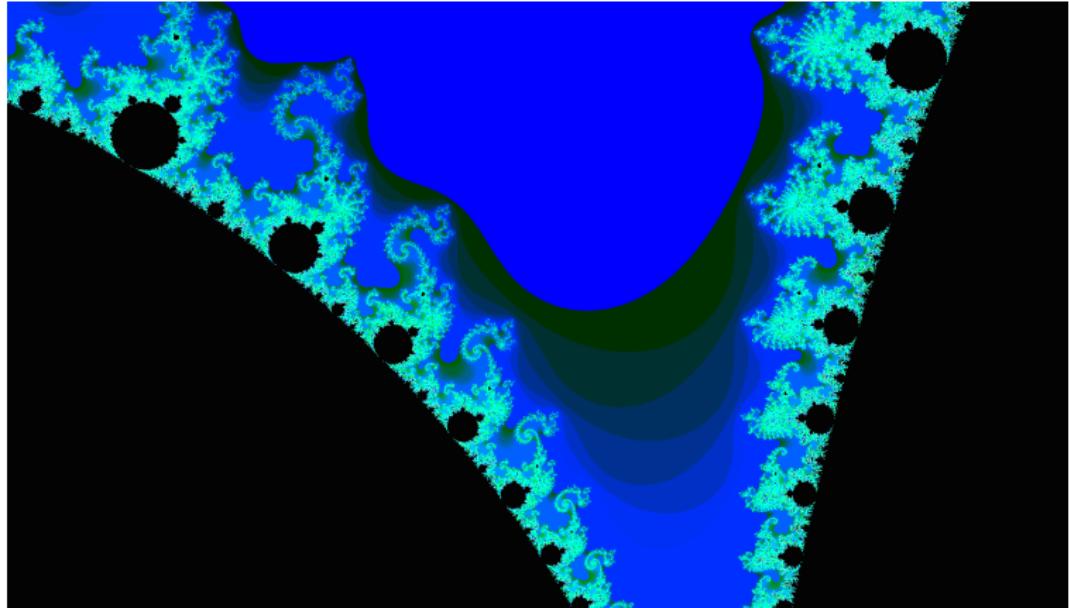
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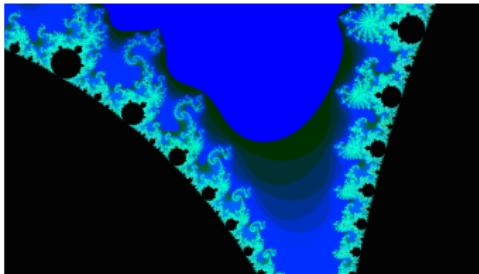
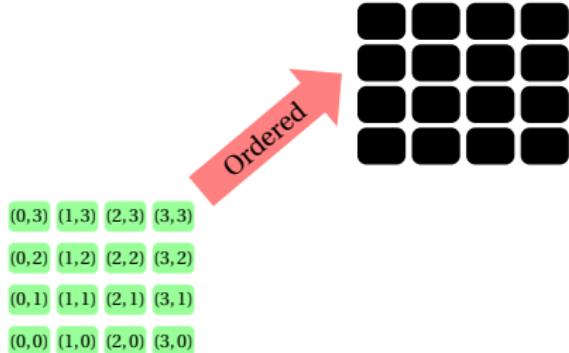
# Functional Map vs. MapReduce



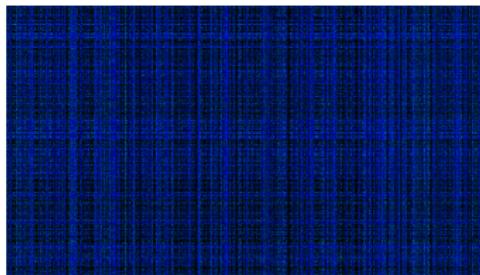
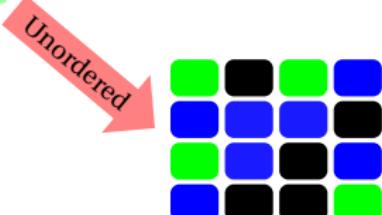
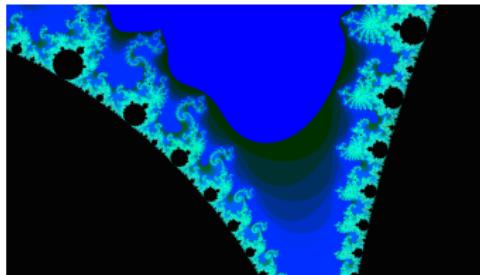
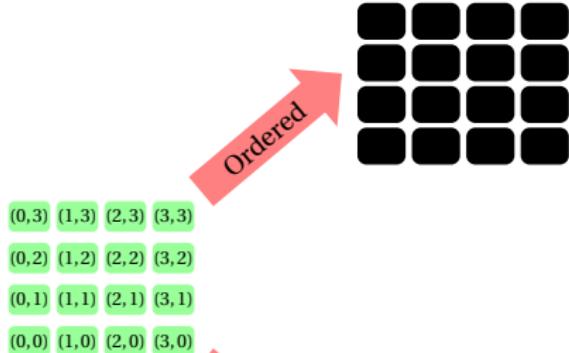
# Functional Map vs. MapReduce

(0,3)	(1,3)	(2,3)	(3,3)
(0,2)	(1,2)	(2,2)	(3,2)
(0,1)	(1,1)	(2,1)	(3,1)
(0,0)	(1,0)	(2,0)	(3,0)

# Functional Map vs. MapReduce



# Functional Map vs. MapReduce



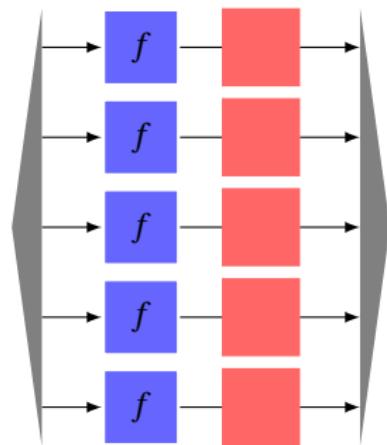
# Structure of a Hardware Implementation

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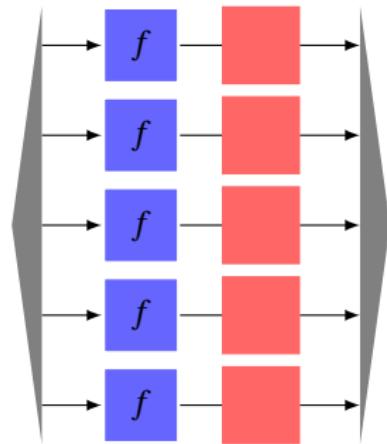
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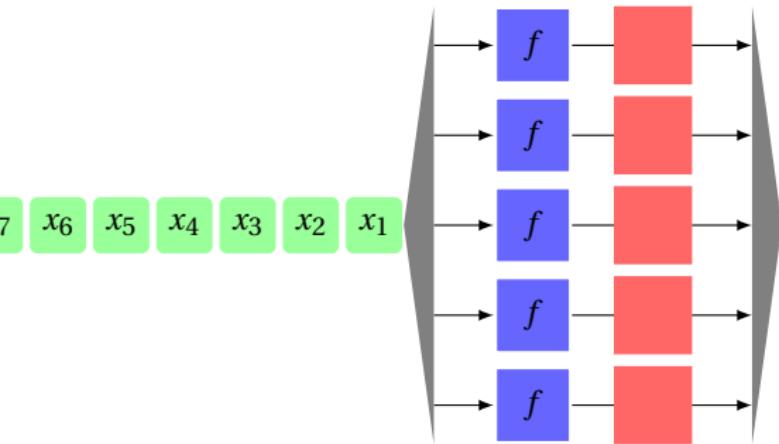


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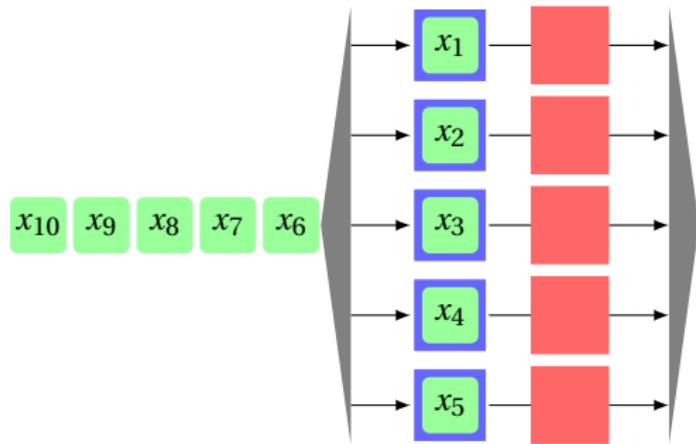


$x_1$   $x_2$   $x_3$   $x_4$   $x_5$   $x_6$   $x_7$   $x_8$   $x_9$   $x_{10}$

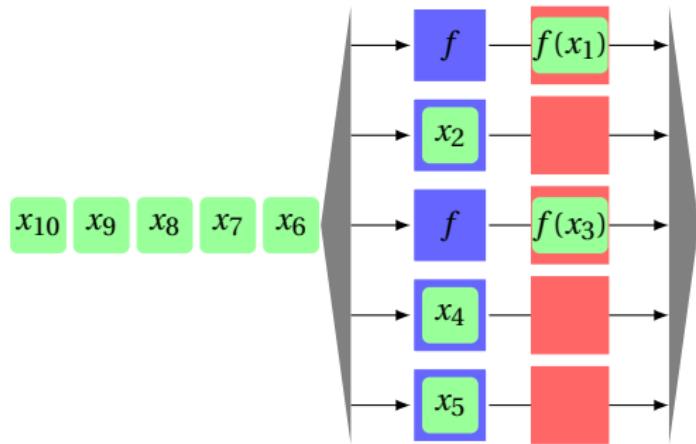
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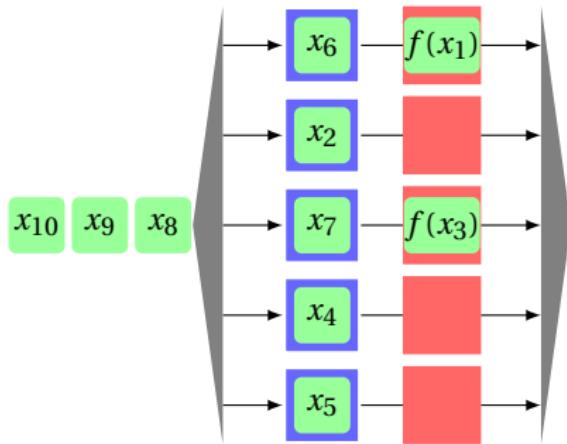
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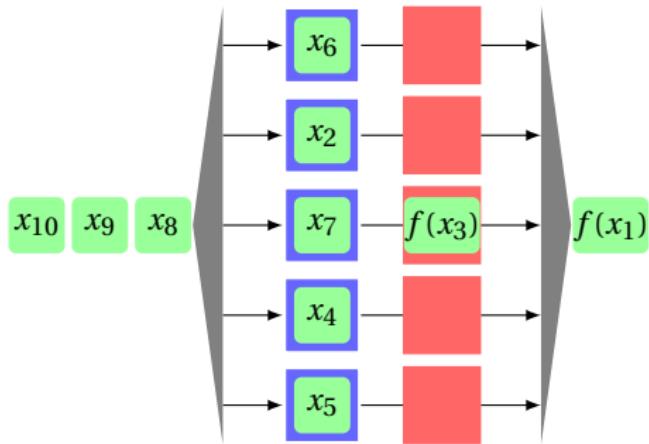
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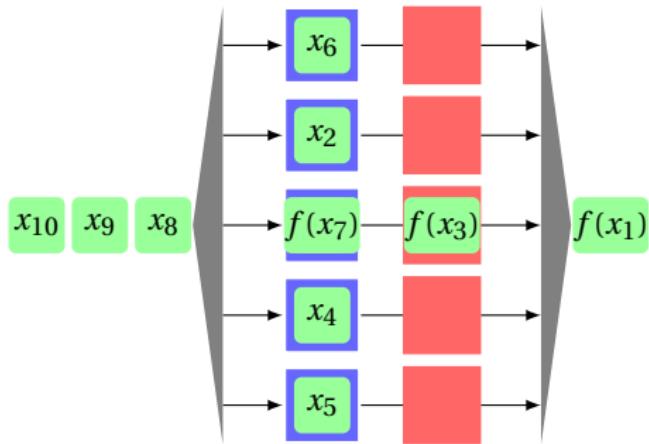
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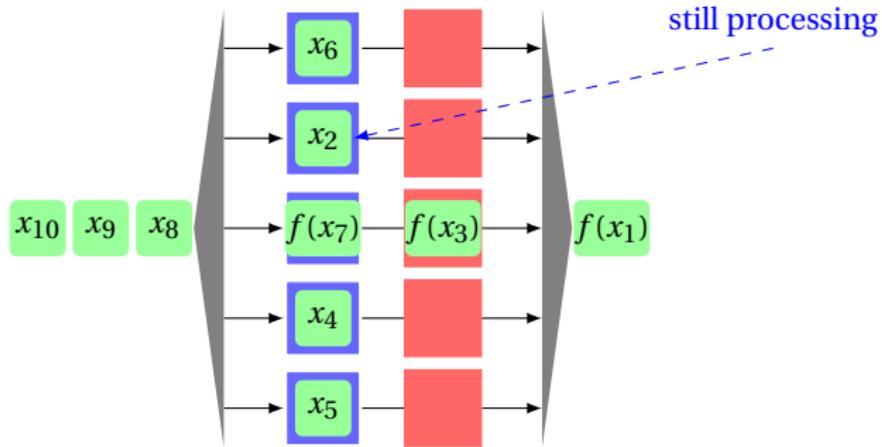
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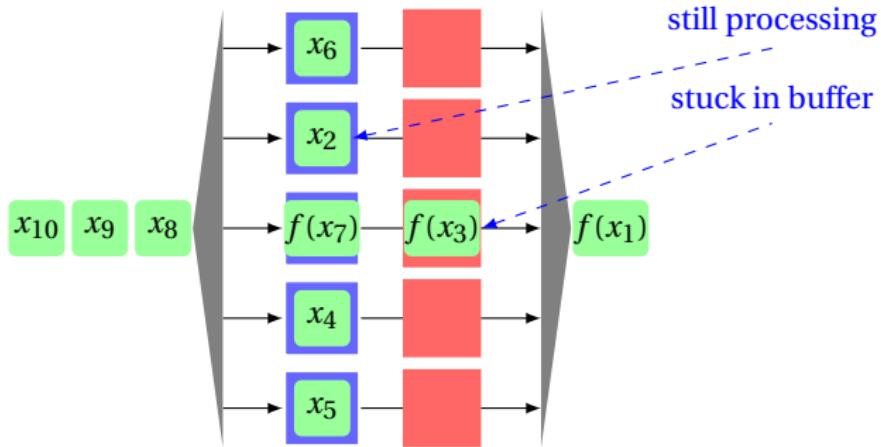
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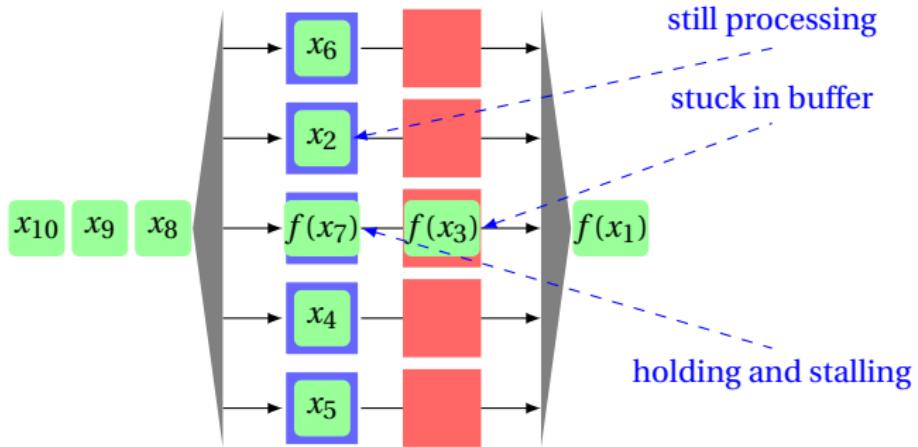
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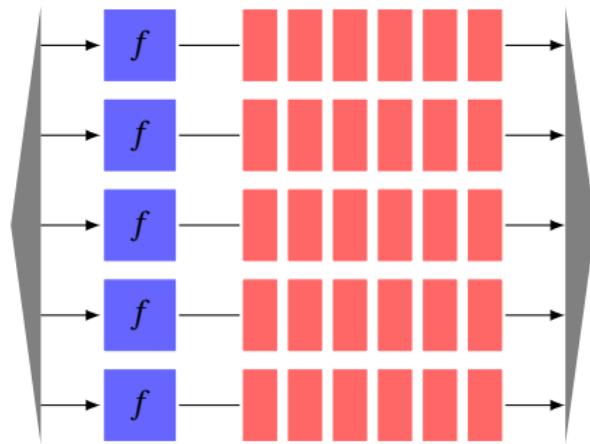
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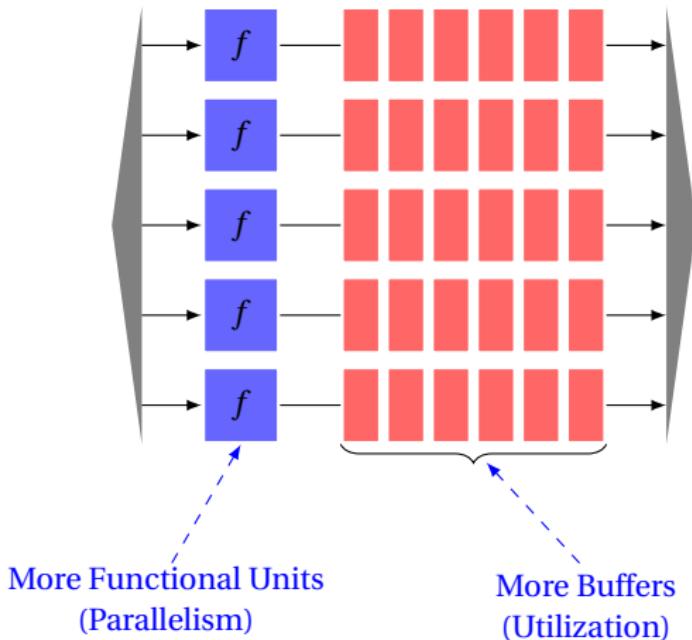
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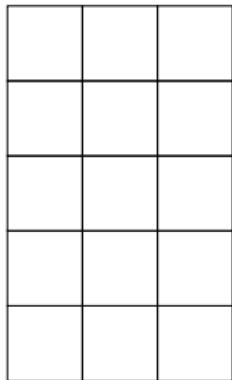
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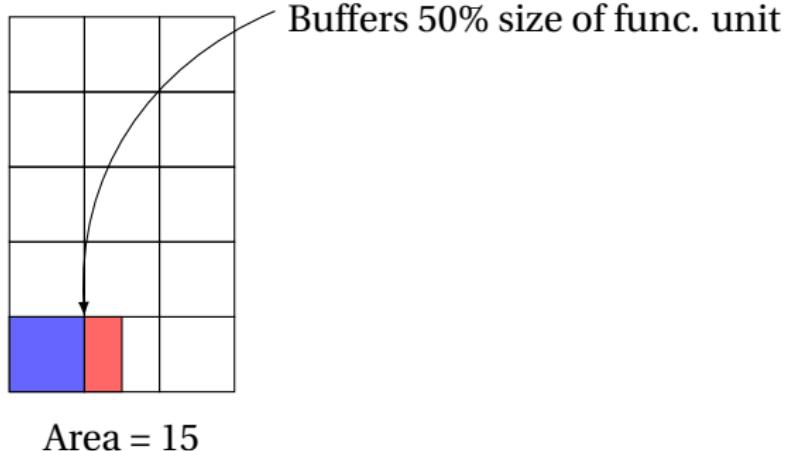


# Multiple Possible Configurations...Which to Choose?

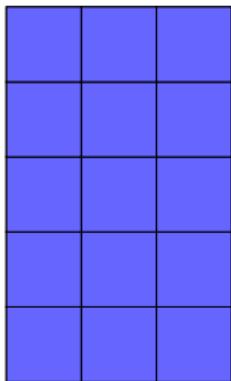


Area = 15

## Multiple Possible Configurations...Which to Choose?

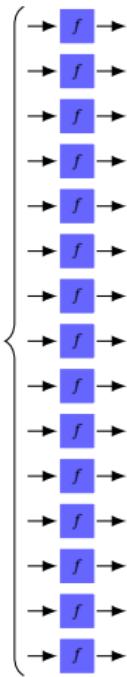


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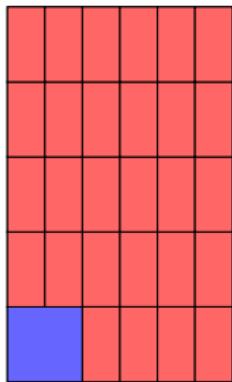


Area = 15

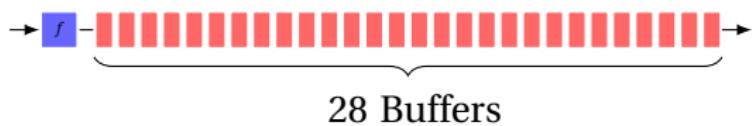
15 Functional Units



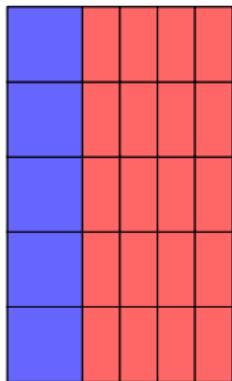
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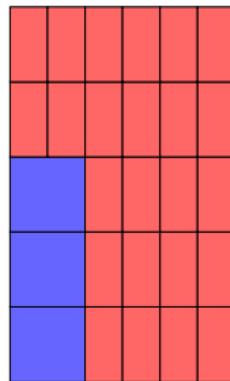
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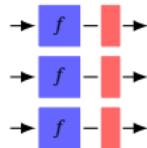
Area = 15



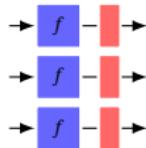
$$5 \left\{ \begin{array}{c} \rightarrow f \rightarrow \text{red} \rightarrow \\ \rightarrow f \rightarrow \text{red} \rightarrow \end{array} \right. \underbrace{\qquad}_{20 \times \frac{1}{2} = 10}$$

$$3 \left\{ \begin{array}{c} \rightarrow f \rightarrow \text{red} \rightarrow \\ \rightarrow f \rightarrow \text{red} \rightarrow \\ \rightarrow f \rightarrow \text{red} \rightarrow \end{array} \right. \underbrace{\qquad}_{24 \times \frac{1}{2} = 12}$$

# Workload Structure



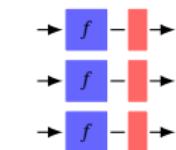
# Workload Structure



Best-case



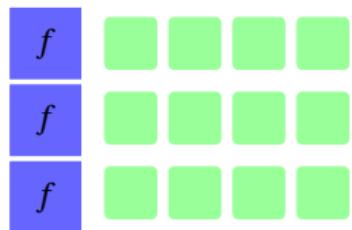
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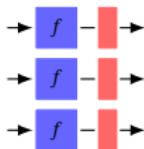
Best-case



Time →



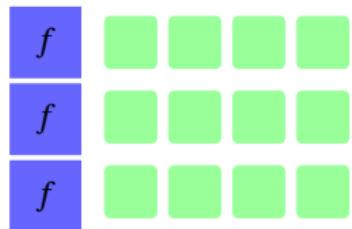
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Best-case



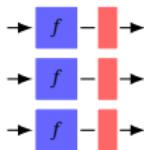
Time →



Average-case

?

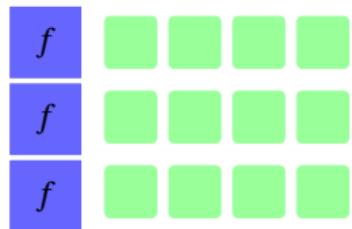
# Workload Structure



Best-case



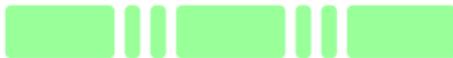
Time →



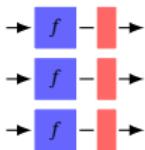
Average-case

?

Worst-case

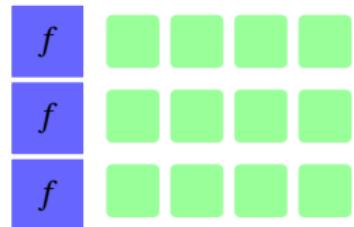


# Workload Structure



Time →

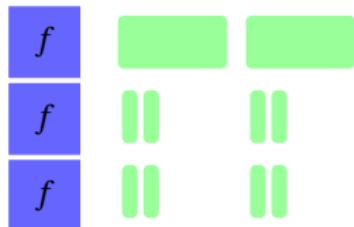
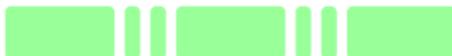
Best-case



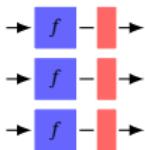
Average-case

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Worst-case



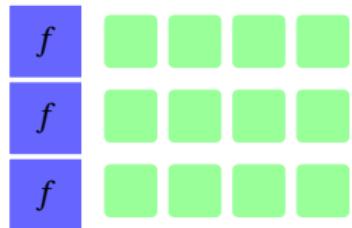
# Workload Structure



Best-case

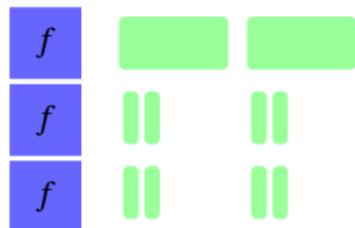
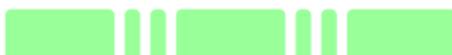


Time →



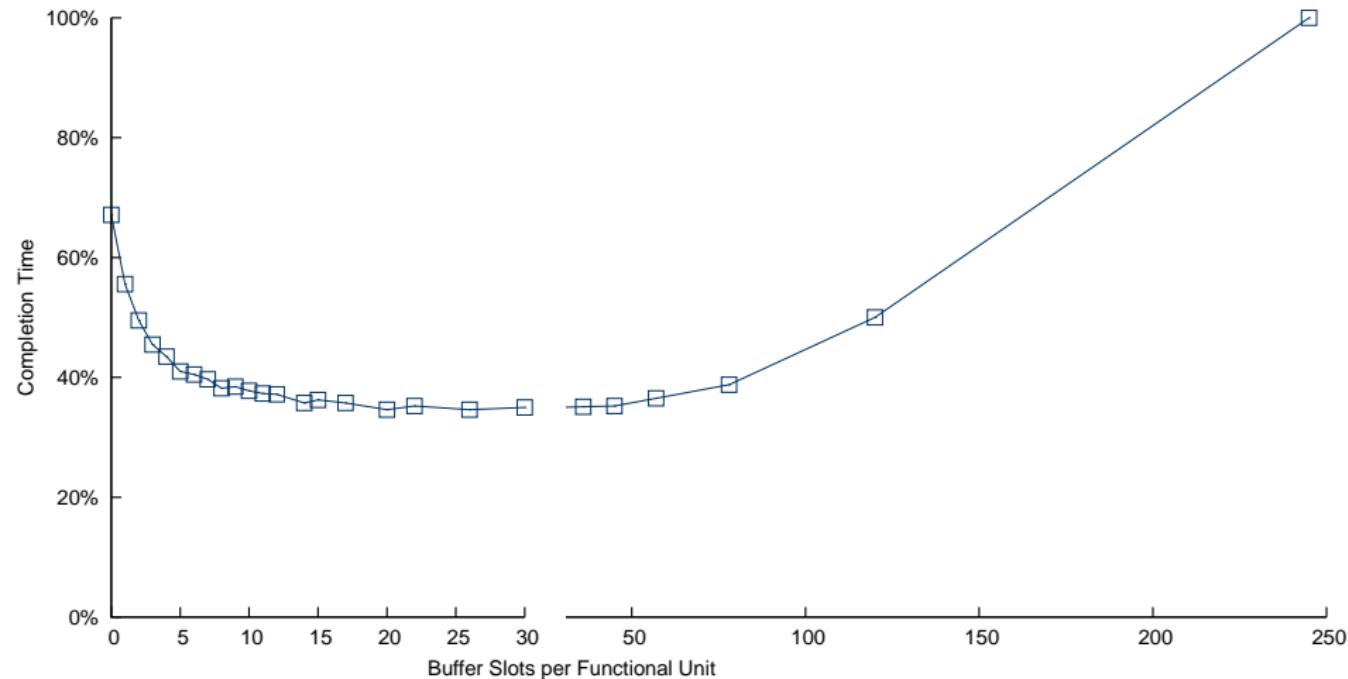
Average-case

?



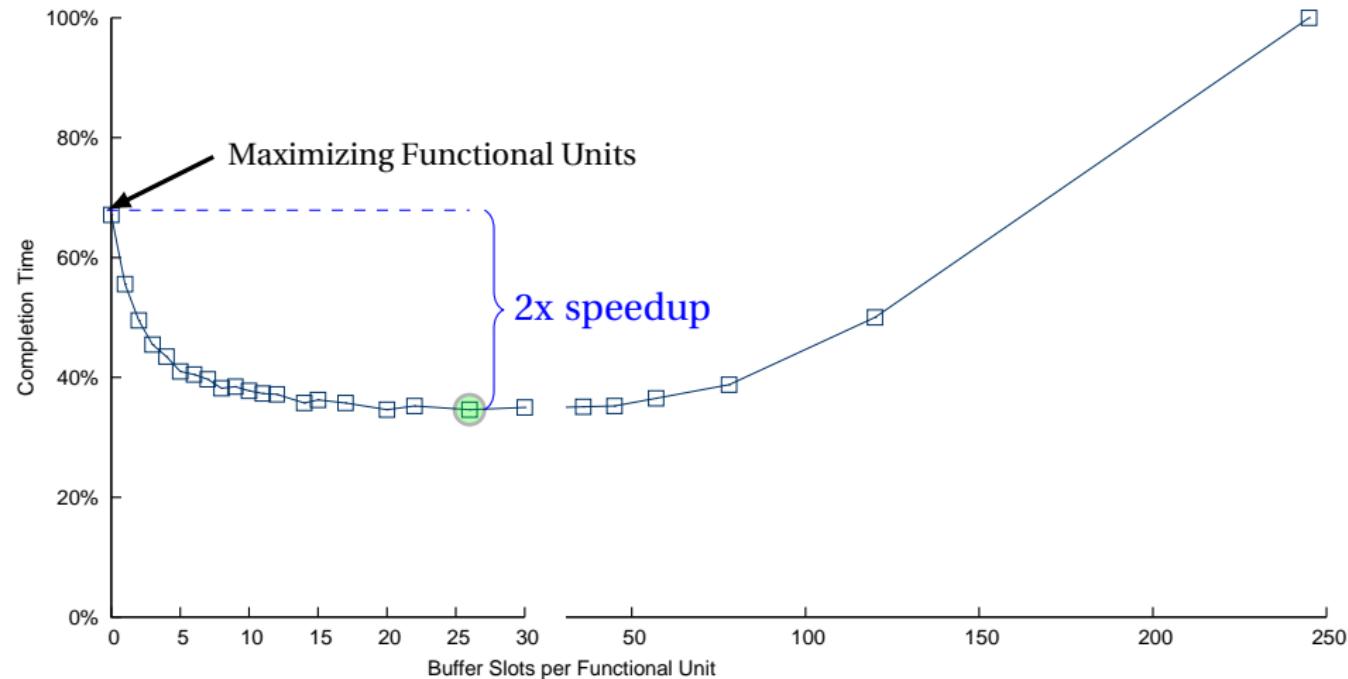
# Optimal Resource Allocation

Simulator Results



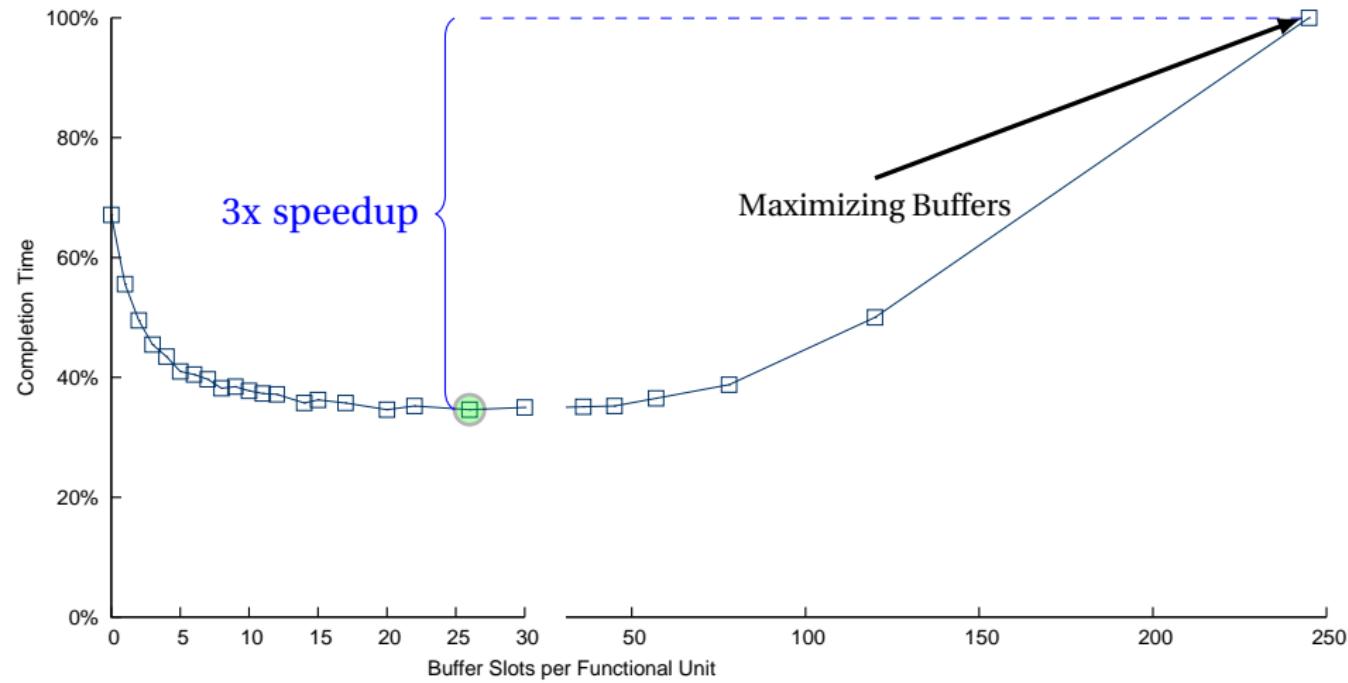
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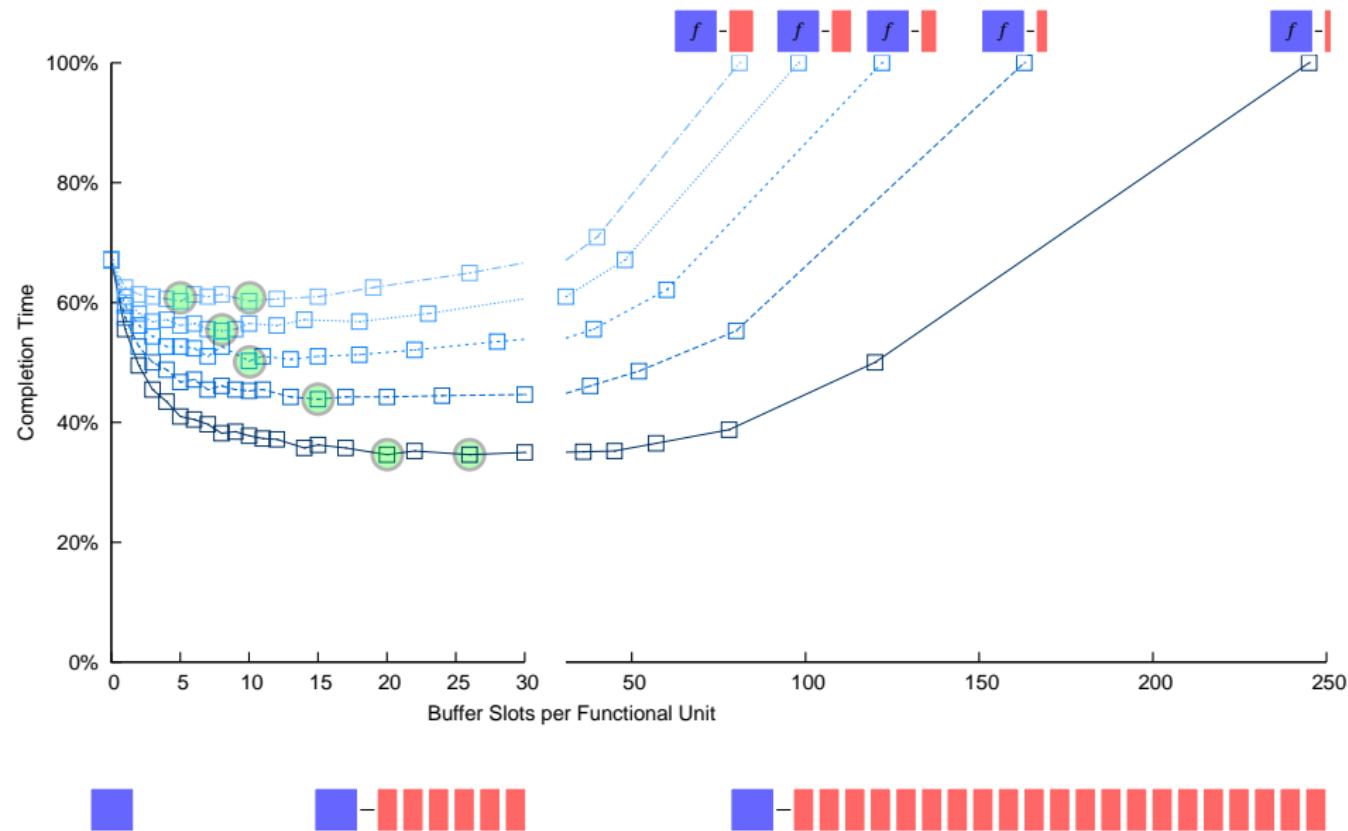


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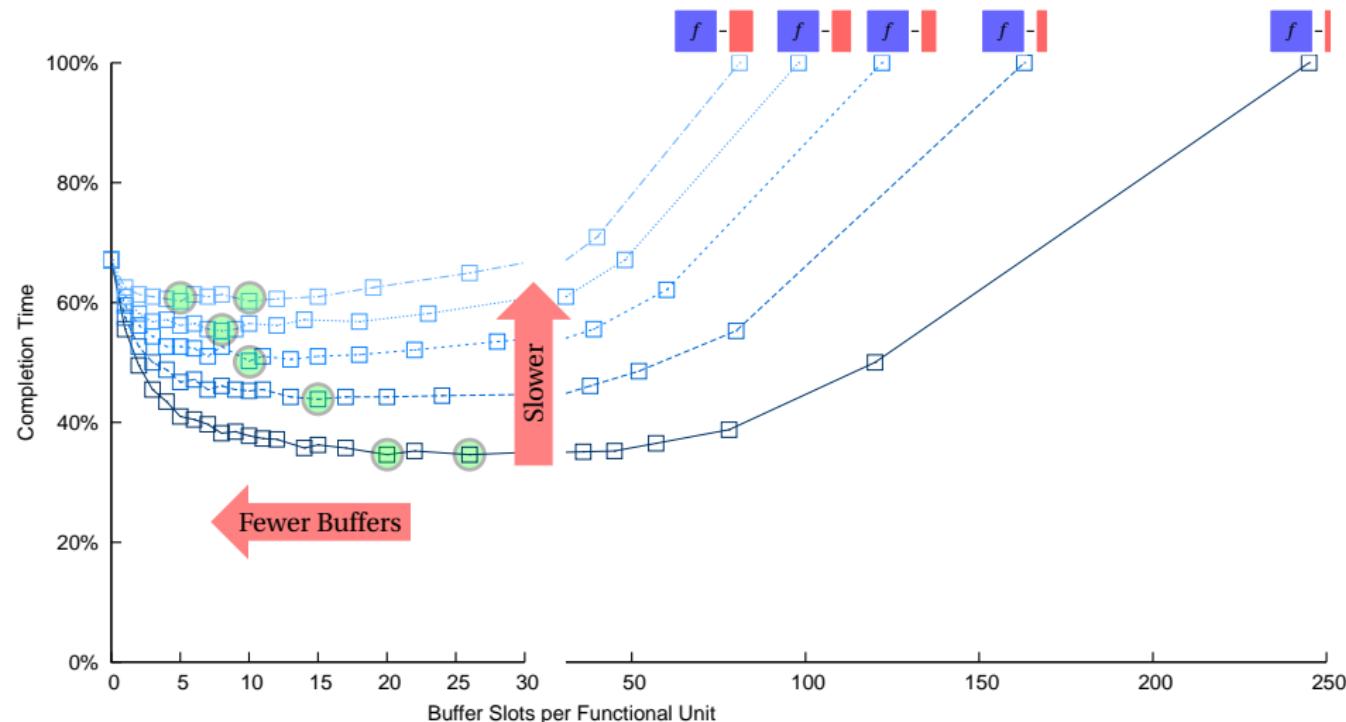
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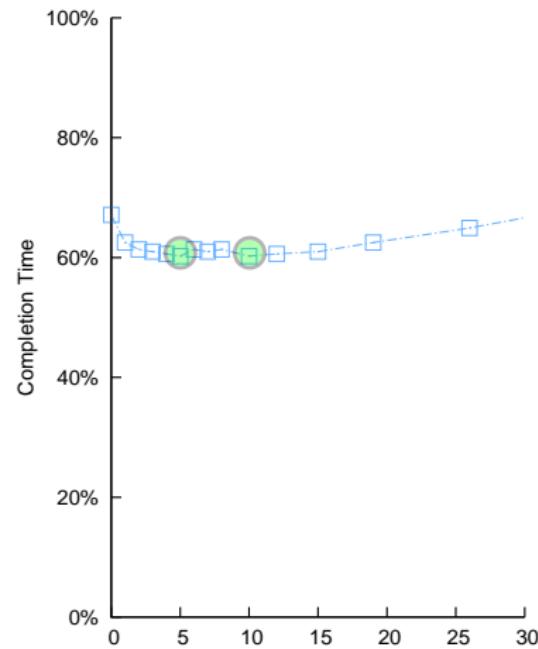
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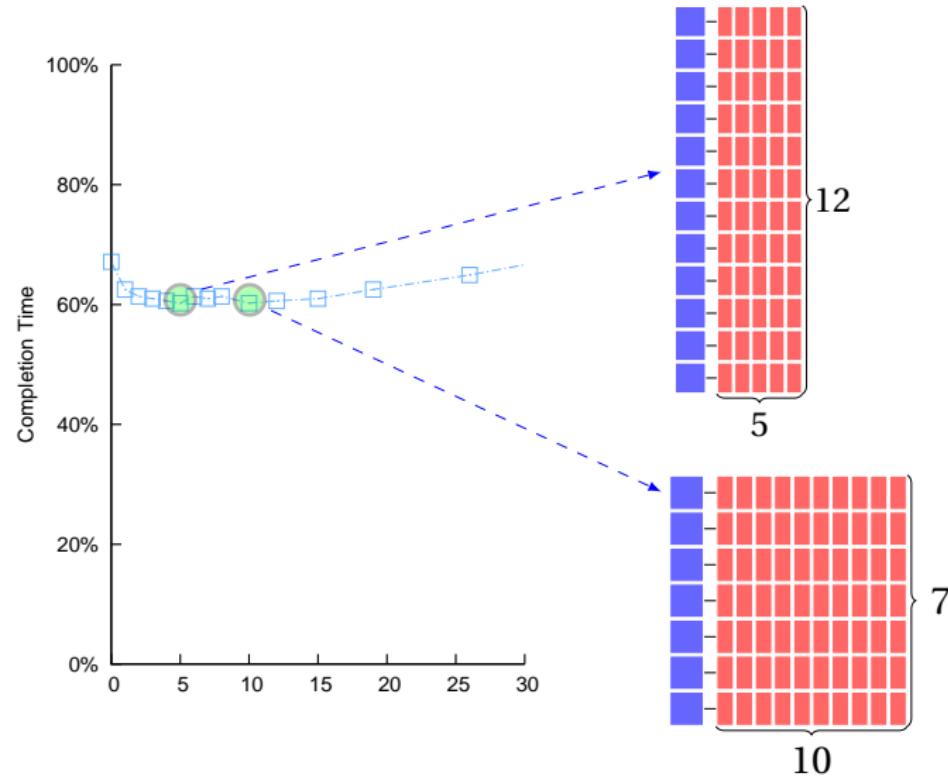
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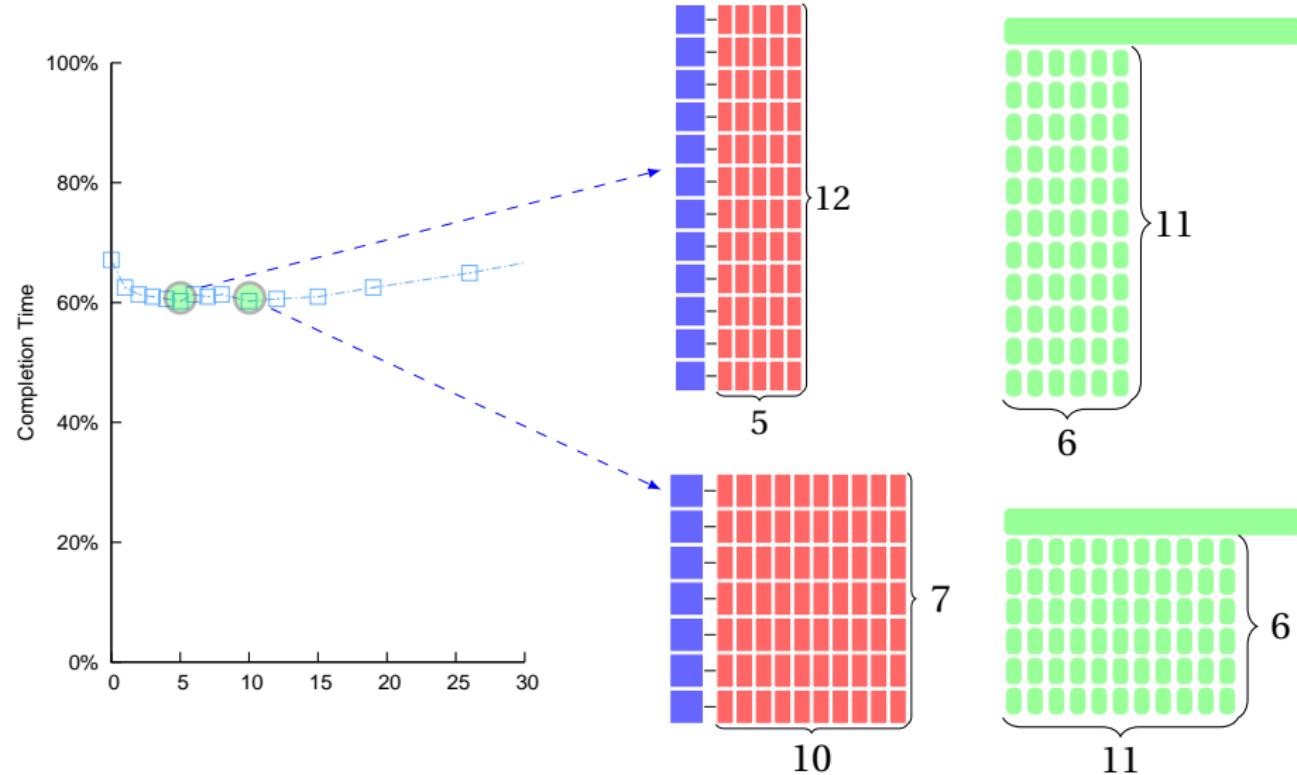
# Why Are There Multiple Optima?



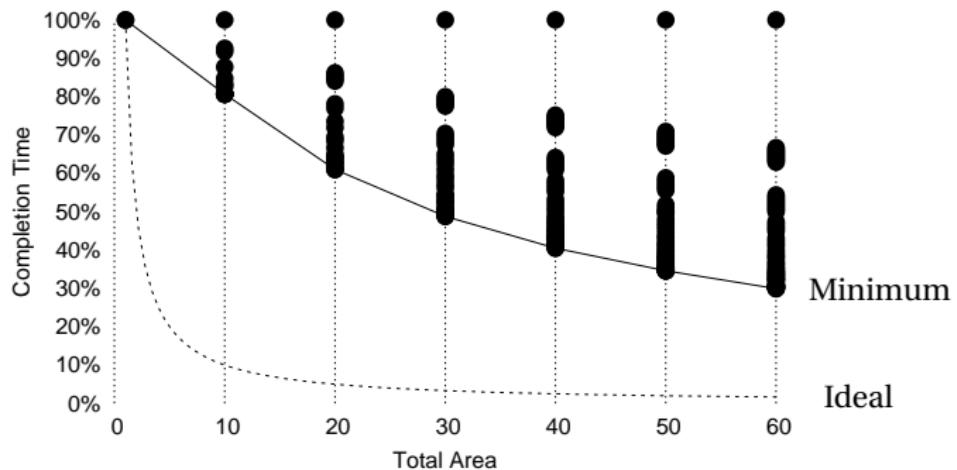
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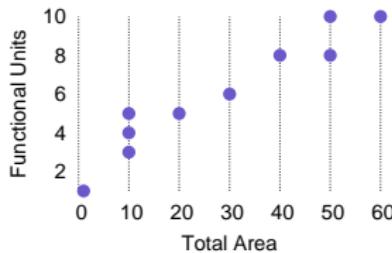
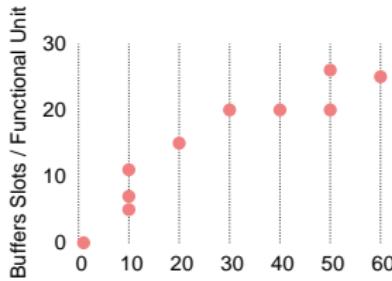
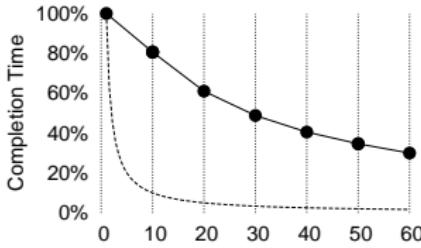
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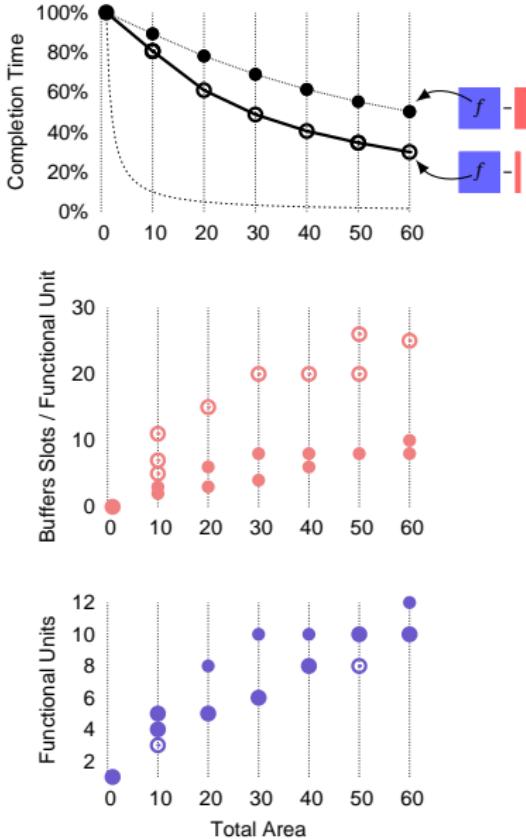
# Performance Scales with Area



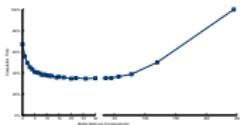
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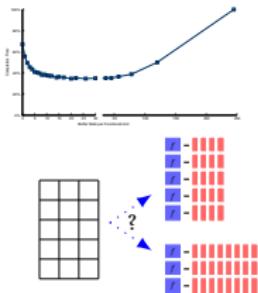


# Conclusions



Area trade-off is important...

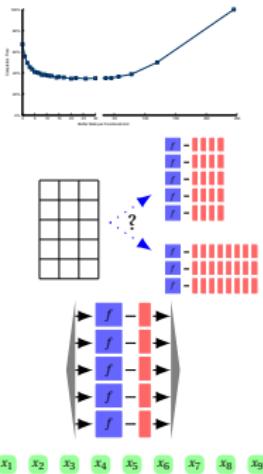
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Area trade-off is important...

...and non-obvious

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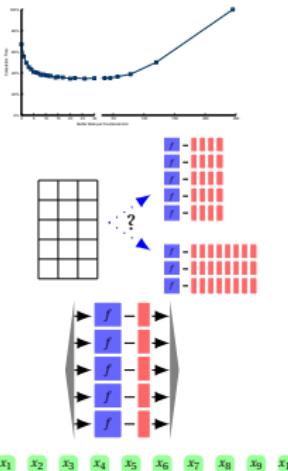


Area trade-off is important...

...and non-obvious

Model helps explore design space

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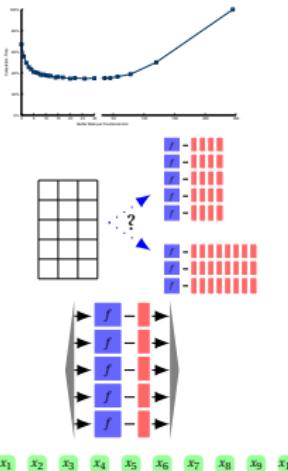
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## Synthesize Efficient Hardware Implementation of Map

# Conclusions

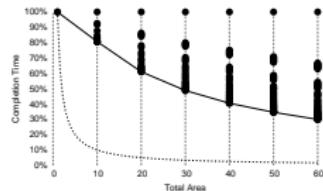


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...and non-obvious

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## Synthesize Efficient Hardware Implementation of Map



Enhance our abstraction